LECTURE 4: RARE DECAYS

Learning goals

- what are rare decays?
- sketch of theory of rare decays
- some 'recent' highlights in rare B decays
 - Bs->mumu
 - Bd->K*gamma
 - lepton-flavour violation tests

Standard Model: "No FCNC at tree level"

CKM: Flavour changing *charged* currents



No Flavour changing *neutral* currents



FCNC at loop level

neutral currents are possible at higher order





- we call them 'rare'
 - higher order
 - often 'GIM suppressed' (cancellation due to unitarity)

Examples of rare decays

• very incomplete table

transition	example of decays
$b \to s\gamma$	$B^0 \to K^{*0} \gamma$
$b \to s \ell^+ \ell^-$	$B_s \to \mu^+ \mu^-, \ B^0 \to K^{*0} \mu^+ \mu^-, \ B^+ \to K^+ \mu^+ \mu^-$
$b \to sq\bar{q}$	$B_d \to K\pi, \ B_s \to \phi\pi$
$b \to d\ell^+\ell^-$	$B^0 \to \rho^0 \mu^+ \mu^-, \ B_d \to \mu^+ \mu^-$
$s \to d\gamma$	$K_L \to \gamma \gamma$
$s \to d\ell^+\ell^-$	$K_L \to \mu^+ \mu^-, \ K_L \to \pi^0 e^+ e^-, \ K^+ \to \pi^0 \mu^+ \mu^-$
$s \to d \nu \bar{\nu}$	$K_L \to \pi^0 \nu \bar{\nu}, \ K^+ \to \pi^+ \nu \bar{\nu}$

• branching fractions typically smaller than $\sim 10^{-5}$, some much much smaller

Effective couplings

• <u>Beta decay</u>: "charged current":



Effective couplings





Dealing with bound states

• consider " $B \rightarrow D \ l \ v$ "

quark level process



$$\mathcal{A}(i \to f) = \langle f | \mathcal{H} | i \rangle$$

$$\Gamma(i \to f) = \int |\mathcal{A}(i \to f)|^2 \, \mathrm{d(phase space)}$$

$$\mathcal{A}(b \to c\ell\bar{\nu}) = \frac{G_F}{\sqrt{2}} V_{cb} \left[\bar{\ell}\gamma^{\mu} (1 - \gamma^5)\nu \right] \left[\bar{c}\gamma_{\mu} (1 - \gamma^5)b \right]$$

Dealing with bound states

• consider " $B \rightarrow D \ l \ v$ "

quark level process



$$\mathcal{A}(b \to c \ell \bar{\nu}) = \frac{G_F}{\sqrt{2}} V_{cb} \left[\bar{\ell} \gamma^{\mu} (1 - \gamma^5) \nu \right] \left[\bar{c} \gamma_{\mu} (1 - \gamma^5) b \right]$$

hadron level process



$$\mathcal{A}(B^0 \to D^+ \ell \bar{\nu}) = \left\langle D^+ \ell \bar{\nu} \right| \mathcal{H} \left| B^0 \right\rangle = ?$$

Dealing with bound states

• sketch of solution (no formal theory!)



General solution: operator product expansion

 approximate H with effective Hamiltonian that integrates out 'all heavy stuff', not just the W, but also the top, etc



General solution: operator product expansion



- Wilson coefficients and matrix elements depend on scale 'mu'
 - computations need to 'match', such that mu-dependence cancels
- matrix elements are hard to compute but effective approximations available: "heavy quark effective theory", "lattice calculations", etc



Rare *B*-decays and effective couplings: $b \rightarrow sl^+l^-$



Effects of 'new physics'

$$\mathcal{A}(i \to f) = \frac{G_F}{\sqrt{2}} \sum_{i} V_i^{\text{CKM}} C_i(\mu) \langle f | O_i(\mu) | i \rangle$$

- new 'heavy' particles only affect scales > mu
 - \rightarrow change Wilson coefficients
- new physics may also lead to local operators that are absent in SM
 - e.g. with scalar bosons or right-handed currents
 - lead to different `kinematics' of final state particles

Fully leptonic

Semi-leptonic

Radiative



Very rare! $\mathcal{B} \lesssim 10^{-9}$

- Theoretically clean
- Mostly clean to reconstruct **Sensitive mainly to** $C_{10}^{(')}$.



• Hadronic pollution.

d

• Mostly clean to reconstruct.

 $K^{(*)0}$

d

• Electron reconstruction very challenging.

Sensitive to $C_7^{(')}$, $C_9^{(')}$ and $C_{10}^{(')}$ depending on $q^2 \equiv m_{\ell^+\ell^-}^2$ region.



- Fairly rare, $\mathcal{B}\sim 10^{-5}$
- Similar to semi-leptonic.
- Experimental resolution not great.

Sensitive to
$$C_7^{(')}$$
.

< ロ > < 団 > < 豆 > < 豆 > < 豆 > < 豆 < つ < ()

(from Riley Henderson at FPCP'23)

Rare *B*-decays and effective couplings: $b \rightarrow s\mu^+\mu^-$

• Effective 4-fermion coupling:

$$\mathcal{H}_{eff} = -\frac{4 G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_{i=1}^{10} \mathcal{C}_i \mathcal{O}_i$$

• Standard Model diagrams:





• Beyond Standard Model:



- Experimental test: Compare calculable C_i coefficients to experimental data
 - Sensitivity for NP in Wilson coefficients C_7 , C_9 , C_{10}

 $B_{s,d} \rightarrow \mu^+ \mu^-$

- very rare decay in SM: FCNC, helicity suppressed
- precise SM calculation (update!)

•
$$B(B_S^0 \to \mu^+ \mu^-) = (3.66 \pm 0.14) \times 10^{-9}$$

• $B(B^0 \to \mu^+ \mu^-) = (1.03 \pm 0.05) \times 10^{-10}$
PRL 112 (2014) 101801
JHEP 10 (2019) 232





- considered very sensitive to new physics (SUSY etc)
- "clean/easy" experimental signature: just count!

Q: why is the Bd decay more rare than the Bs decay?



 $B_s: V_{ts} V_{tb}^*$

 $B_d: V_{td} V_{tb}^*$



 $B_{s,d} \rightarrow \mu^+ \mu^-$

• observed signals at the LHC:



note the importance of good mass resolution!

 $B_{s,d} \rightarrow \mu^+ \mu^-$



- good agreement between experiment and theory
- non-SM contributions not much more than 15%
 - → strong contraints on BSM physics
- no clear evidence yet for Bd->μμ

 $B_d \rightarrow K^{*0} \mu^+ \mu^-$ (and alike)



 invariant mass-squared of μμ pair is called "q-squared":

$$q^2 = \left| p^{\mu}(\ell^+) + p^{\mu}(\ell^-) \right|^2$$

Contribution of operators depends on q^2







• Branching fractions related to $b \rightarrow s \ \mu^+ \mu^-$ transition *consistently lower* than predicted.

Angular distributions

• in >2-body decays, also "angular distributions" sensitive to NP



- experimental challenge: backgrounds and angular efficiency
- theoretical challenge: choose observables with small hadronic uncertainties

Example: angular distributions in $B^0 \rightarrow K^{*0} \mu \mu$





- global fits: perform fits so all b->sll data, allowing for NP contributions to Wilson coefficients
- the fit seems to indicate new contributions to 'C9'
- the 'pull' of the SM is about 4 sigma

Lepton universality

- SM: all leptons have 'universal couplings'
- well tested with $W^{\pm} \rightarrow l^{\pm}\nu$ and $Z^0 \rightarrow l^+l^-$ (e.g. at LEP and SLC)

for example, branching fractions of Z to leptons from PDG:

Γ_1	<i>e</i> ⁺ <i>e</i> ⁻	[1]	$(3.3632 \pm 0.0042)\%$
Γ_2	$\mu^+\mu^-$	[1]	$(3.3662\pm 0.0066)\%$
Γ_3	$ au^+ au^-$	[1]	$(3.3696 \pm 0.0083)\%$

 meson decays provide additional tests, e.g. sensitivity to new forces between quarks and leptons ("lepto-quarks")

B-decays and lepton universality

• $b \rightarrow c \ l \ v$ charged current: "Allowed" \rightarrow large decay rates







R_D and R_{D^*}

• $b \rightarrow c \, l \, v$ allowed charged current (tree level)

$$R(D^{(*)}) = \frac{BR(B \to D^{(*)}\tau\nu)}{BR(B \to D^{(*)}\mu\nu)}$$

→Involves leptons of 2nd and 3rd generation





•
$$b \rightarrow s \, l^+ l^-$$
 suppressed neutral current
 $R(K) = \frac{BR(B^+ \rightarrow K^+ \mu^+ \mu^-)}{BR(B^+ \rightarrow K^+ e^+ e^-)}$
 $R(K^*) = \frac{BR(B^0 \rightarrow K^* \mu^+ \mu^-)}{BR(B^0 \rightarrow K^* e^+ e^-)}$
• caused some excitement in past, because LHCb seemingly found deviations from 1

latest LHCb results are perfectly
 Interview of the set of the



$$R_{K} \text{ and } R_{K}^{*}$$
• $b \rightarrow s l^{+}l^{-}$ suppressed neutral current

$$R(K) = \frac{BR(B^{+} \rightarrow K^{+}\mu^{+}\mu^{-})}{BR(B^{+} \rightarrow K^{+}e^{+}e^{-})}$$

$$R(K^{*}) = \frac{BR(B^{0} \rightarrow K^{*}\mu^{+}\mu^{-})}{BR(B^{0} \rightarrow K^{*}e^{+}e^{-})}$$
• Involves leptons of 1st and 2nd generation
• situation until 2022: >3 sigma deviation from expectation



Underestimated background:





R_K and R_{K^*}

• $b \rightarrow s \ l^+l^-$ suppressed neutral current



with expectation *in this observable*

why we should keep testing "Lepton universality"

Suppose we could test matter only with long wave-length photons...



We would conclude that these two particles are "<u>identical copies</u>" <u>but for their mass</u> ...

This is exactly the same (*potentially misleading*) argument we use to infer LFU in the SM...



These three (families) of particles seems to be "<u>identical copies</u>" <u>but for their mass</u> ...

The SM quantum numbers of the three families could be an "accidental" <u>low-energy</u> <u>property</u>: the different families may well have a very different behavior at high energies, as <u>signaled by their different mass</u>

Isidori, 2019

Implications for low-energy flavor physics

If the anomalies are due to NP, we should expect to see several other BSM effects in low-energy observables

E.g.: correlations among down-type FCNCs [using the results of U(2)-based EFT]:

	μμ (ee)	ττ	νν	τμ	μe
$b \rightarrow s$	R _K , R _{K*}	$B \rightarrow K^{(*)} \tau\tau$ $\longrightarrow 100 \times SM$	$B \rightarrow K^{(*)} vv$ $O(1)$	$B \to K \tau \mu$ $\longrightarrow \sim 10^{-5}$	$ \begin{array}{c} \mathbf{B} \to \mathbf{K} \ \mu \mathbf{e} \\ \hline ??? \end{array} $
$b \rightarrow d$	$B_{d} \rightarrow \mu\mu$ $B \rightarrow \pi \mu\mu$ $B_{s} \rightarrow K^{(*)} \mu\mu$ $O(20\%) [R_{K}=R_{\pi}]$	$\begin{array}{c} B \rightarrow \pi \ \tau\tau \\ \hline \rightarrow 100 \times SM \end{array}$	$B \rightarrow \pi \nu \nu$ $O(1)$	$B \rightarrow \pi \tau \mu$ $\longrightarrow \sim 10^{-7}$	$B \rightarrow \pi \mu e$ $???$
$s \rightarrow d$	long-distance pollution	NA	$K \rightarrow \pi vv$ $O(1)$	NA	K → μe ???

S. Fajfer, ICHEP2018

Models at TeV scale explaining both B anomalies

Scalar LQ as pseudo-Nambu-Goldstone boson	Vector resonances (from techni-fermions)			
Gripaios et al, 1010.3962, Gripaios et al., 1412.1791, Marzocca 1803.10972	Barbieri et al.,1506.09201, Buttazzo et al. 1604.03940, Barbieri et al., 1611.04930 Blanke & Crivellin, 1801.07256,			
Models with scalar LQs Hiller & Schmaltz, 1408.1627,	Gauge bosons			
Becirevic et al. 1608.08501, SF and Kosnik, 1511.06024, Becirevic et al., 1503.09024,	Greljo et al., 1804.04642 Cline, Camalich, 1706.08510			
Dorsner et al, 1706.07779, Cox et al., 1612.03923, Crivellin et al.,1703.09226	Calibbi et al.,1709.00692 Assad et al., 1708.06350 Di Luzio et al.,1708.08450			

Bordone et al.,1712.01368, 1805.09328...

W', Z' in warped space

Megias et al., 1707.08014

Some of the things that I did not course

- CP violation and rare decays in the Kaon sector
- lepton-number violation (e.g. $\mu \rightarrow e\gamma, \mu \rightarrow eee$)
- electric dipole moments
- g-2
- majorana neutrinos
- ...



Closing remarks

- low energy measurements can be sensitive to very high mass scales
- several 'quark flavour physics' measurements show tension with SM predictions
 - experimental effects?
 - theoretical understanding?
 - new physics?
 - \rightarrow Belle-II/LHC measurements will improve a lot over coming decade
- lot's of other exciting experiments ongoing: watch tight!