



Beaming patterns of Neutrino Emission from Blazars

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Origin of IceCube-Detected Neutrinos



Significant correlation of IceCube neutrinos with γ -ray (Fermi-LAT) **blazars** (chance coincidence probability p = $6 \cdot 10^{-7}$)

- but can not be responsible for all IceCube neutrinos (e.g., Murase et al. 2018)

Origin of IceCube-Detected Neutrinos



Also: Correlation with radio-loud blazars (chance-coincidence probability of p = 3·10⁻⁴) (Plavin et al. 2020, 2021, 2022)

Photo-Pion Production Cross Section

 Δ^+ resonance (1232 MeV)





Center-of-Momentum energy

For realistic target photon fields, most interactions occur near threshold (at Δ^+ resonance).

Interaction Probability

Photo-pion production - Energetics

At Δ^+ resonance:

s =
$$E_p' E_t' (1 - \beta_p' \chi) = E_{\Delta^+}^2 = (1232 \text{ MeV})^2$$

Each neutrino takes about ~ 5 % of the proton's energy

 \Rightarrow To produce IceCube neutrinos (~ 100 TeV \rightarrow $E_v = 10^{14} E_{14} eV$):

Need protons with $E'_p \sim 200 E_{14} \delta_1^{-1} \text{ TeV}$ and target photons with $E'_t \sim 1.6 E_{14}^{-1} \delta_1 \text{ keV}$

<u>Photo-pion production –</u> <u>Origin of Target Photons</u>

To produce IceCube neutrinos (~ 100 TeV \rightarrow E_v = 10¹⁴ E₁₄ eV):

Need protons with

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and target photons with $E'_t \sim 1.6 E_{14}^{-1} \delta_1 \text{ keV} => X-rays!$

(At least) two possible scenarios:

- a) <u>Target photons co-moving</u> with the emission region
- \Rightarrow E_t^{obs} ~ 16 E₁₄⁻¹ δ_1^2 /(1+z) keV
- ⇒ Observed as Doppler-boosted hard X-rays
- Tightly constrained by observed hard X-ray flux -> Energetics constraints.

- b) <u>Target photons stationary in</u> <u>the AGN frame</u>
- $\Rightarrow E_t^{obs} \sim 160 E_{14}^{-1}/(1+z) eV$
- ⇒ Observed as UV / soft X-rays, Doppler boosted into the emission-region frame

Much more relaxed energetics constraints.

<u>Photo-pion production –</u> <u>Origin of Target Photons</u>

Possible sources of external UV / soft X-ray target photons:



<u>Neutrino production on external</u> <u>target photon fields</u>

- Assume target photon field isotropic in the AGN rest frame.
- Highly anisotropic in the co-moving (blob) frame.
- Assume $p\gamma$ interactions only at the Δ^+ resonance:

 $E_t E_p (1 - \beta_p \chi) = E_{\Delta}^2$ with χ = cosine of interaction angle => In blob frame:

 $E_p \approx 20 E_v; \qquad E_t \approx E_{\Delta}^2 / (20 E_v [1 - \beta_p \chi])$

- Hugely dominant proton momentum => $\widehat{\Omega}_{proton} = \widehat{\Omega}_{neutrino}$
- Efficient head-on collisions for neutrino production along the jet axis.
- Expect significantly stronger Doppler boosting and beaming than for co-moving target photon field (see Dermer 1995 for similar effect on external-Compton scattering)

Evaluation of neutrino beaming patterns (I)

• Relevant quantity: Neutrino number flux:

$$\Phi_{\nu} \left(\Omega_{obs}\right) = \int_{E_{\nu,1obs}}^{E_{\nu,2obs}} \Phi_{\nu,Eobs} dE_{\nu}^{obs} = \frac{\delta^3 \left(1+z\right)}{4\pi d_L^2} V_b \int_{E_{\nu,1}}^{E_{\nu,2}} \dot{n}_{E_{\nu}} \left(\Omega\right) dE_{\nu}$$
with $\mu = \frac{\mu_{obs} - \beta_{\Gamma}}{1 - \mu_{obs} \beta_{\Gamma}}$ and $E_{\nu}^{obs} = \delta E_{\nu}$.
 $\dot{n}_{E_{\nu}} \left(\Omega\right) \propto \int_{-1}^{1} d\mu_t \int_{0}^{2\pi} d\varphi_t n_t (E_t, \Omega_t) n_p (E_p) (1 - \beta_p \chi)$

with
$$\chi = \widehat{\Omega}_t \cdot \widehat{\Omega}_p = \widehat{\Omega}_t \cdot \widehat{\Omega}_v$$

Evaluation of neutrino beaming patterns (II)

Assume simple power-law proton and photon spectra:

$$n_p(E_p) \propto E_p^{-p}$$
 and $n_t(E_t) \propto E_t^{-\alpha}$

<u>Photon field isotropic in</u> <u>co-moving frame (internal)</u>

$$n_t(E_t, \Omega_t) = \frac{n_t(E_t)}{4\pi}$$

<u>Photon field isotropic in</u> <u>AGN frame (external)</u>

$$n_t(E_t, \Omega_t) = \frac{n_t^{*}(E_t^{*})}{4\pi \, \delta_*^{2}}$$

with $\delta_* = \Gamma \left(1 + \beta_{\Gamma} \mu_t\right)$

Results shown for full numerical angle integration.

Analytical approximations to beaming patterns

Internal target photon field

Set
$$\beta_p = 1$$
, $\chi = -1$

 $\Rightarrow \Phi_{\nu} \left(\Omega_{obs} \right) \propto \delta^{2 + p - \alpha}$

External target photon field

Set
$$\beta_p = 1$$
, $\mu_t = -1$
=> $\chi = -\mu$

$$\Rightarrow \Phi_{\nu} (\Omega_{obs}) \propto \delta^{2+p} (1+\mu_{obs})^{\alpha}$$



<u>Dependence of beaming patterns</u> <u>on Lorentz factor</u>

Internal target photon field

External target photon field

 $\Phi_{\nu}\left(\Omega_{obs}\right) \propto \delta^{2+p-\alpha}$

 $\Phi_{\nu} \left(\Omega_{obs} \right) \propto \delta^{2+p} \left(1 + \mu_{obs} \right)^{\alpha}$



<u>Dependence of beaming patterns</u> <u>on spectral indices</u>

Internal target photon field

External target photon field

 $\Phi_{\nu}\left(\Omega_{obs}\right) \propto \delta^{2+p-\alpha}$

 $\Phi_{\nu} \left(\Omega_{obs} \right) \propto \delta^{2+p} \left(1 + \mu_{obs} \right)^{\alpha}$



<u>Summary</u>

- Production of IceCube neutrinos in blazar jets requires target photons of co-moving UV / X-ray energies, most plausibly from outside the jet
- Doppler boosting and beaming of neutrino production on external target photon fields are much narrower and stronger than for co-moving isotropic target fields.
- Look for the most closely aligned blazars as most promising neutrino blazars.
- Neglecting detailed beaming patterns might under-estimate the neutrino flux by huge factors (~ 10^6 for Γ = 20) and, conversely, over-estimate power requirements.





