



Hadronic interactions in Angantyr

Marius Utheim

in collaboration with Ilkka Helenius

Wuppertal, January 22nd, 2024

Outline

Background

Modelling

Results

Summary and outlook

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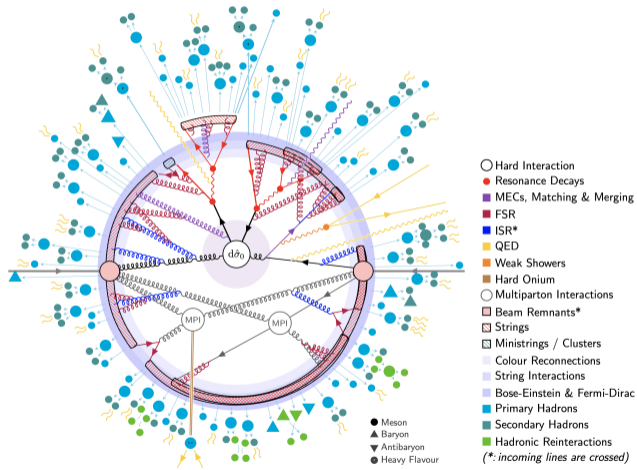
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Summary and outlook

Pythia and Angantyr

PYTHIA is a general-purpose event generator.

- ▶ For information about PYTHIA itself, see Torbjörn's talk from earlier
- ▶ In this talk, I focus on ANGANTYR, the module for heavy ions.



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Hadron-proton interactions already exist in PYTHIA [[arXiv:2108.03481](https://arxiv.org/abs/2108.03481)]. In this talk, I will present this framework, then introduce the changes we have made to extend this to ANGANTYR. Finally we look at some results, comparing to HERA and LHC data.

Cosmic rays

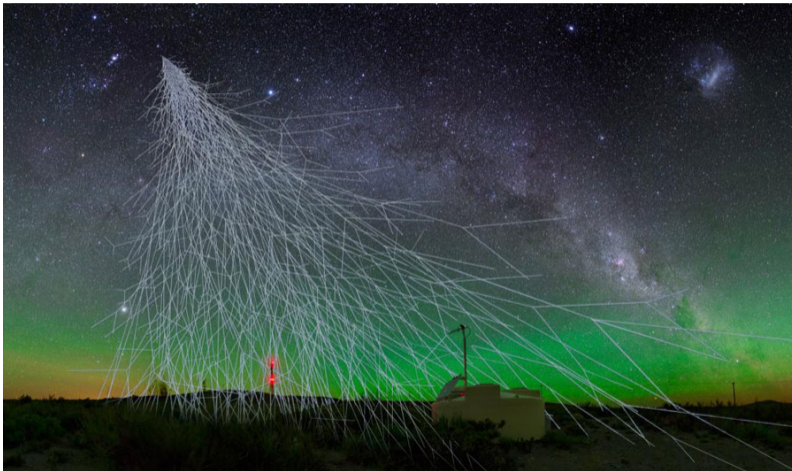


Photo-induced processes

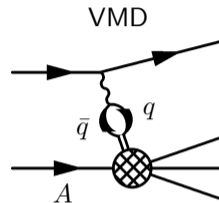
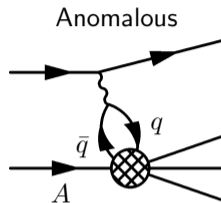
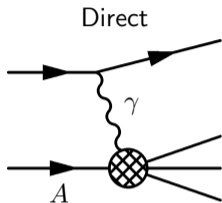


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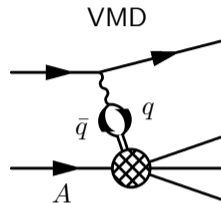
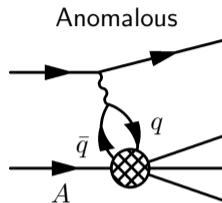
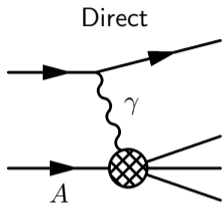
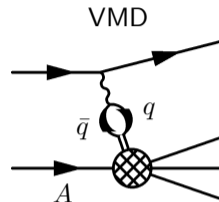
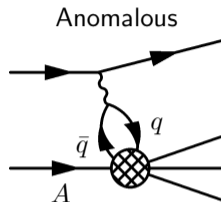
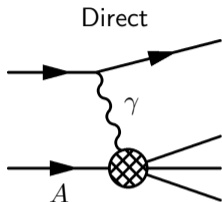
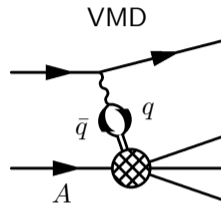
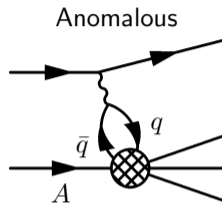
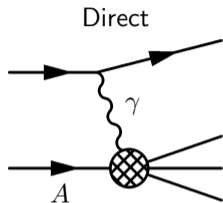


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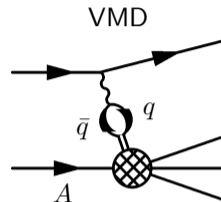
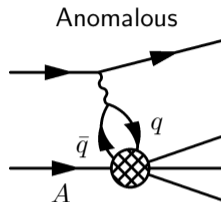
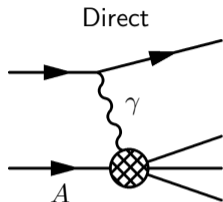
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- ▶ The anomalous part is more complicated. The q and \bar{q} can interact with different nucleons in A .
- ▶ The VMD part can be described as a hA interaction, analogous to pA . This is the component with highest multiplicity, due to MPIs and multiple subcollisions.

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Total and partial cross sections

Several models for total cross sections are available in Pythia. The most generic is the Donnachie-Landshoff model, which is available for most hadron–nucleon combinations:

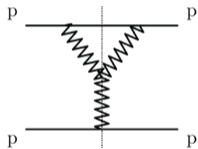
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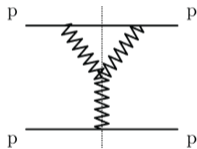
$$d\sigma = \frac{g_{3P}\beta_{AP}\beta_{BP}^2}{16\pi} \frac{dM_X^2}{M_X^2} (e^{B_{XB}t} dt) F_{SD}(M_X^2, s)$$

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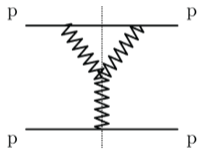
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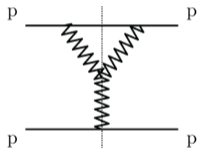
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- ▶ $B_{XB} = 2b_B + 2\alpha'_{\mathbb{P}} \log(s/M_X^2)$ with $b = 1.4$ for mesons and 2.3 for baryons

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- ▶ $B_{XB} = 2b_B + 2\alpha'_P \log(s/M_X^2)$ with $b = 1.4$ for mesons and 2.3 for baryons
- ▶ F_{SD} is a fudge factor (out of scope for this talk)

Parton distribution functions

PDFs determine the contents of a hadron. For protons, detailed PDFs based on global fits exist, the Pythia default being NNPDF2.3 QCD+QED LO (with $\alpha_S = 0.130$).

Parton distribution functions

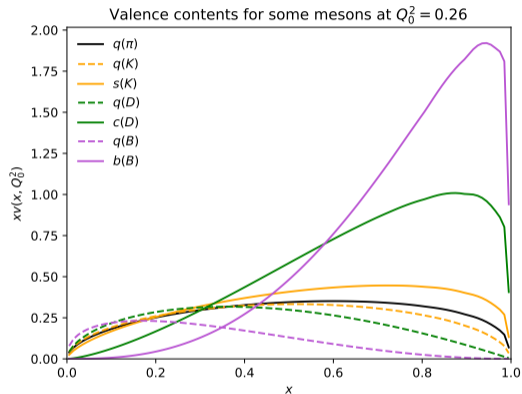
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For other species, very little data exists, and we base our valence distributions on an ansatz by Glück, Reya et al. [[arXiv:hep-ph/9806404](https://arxiv.org/abs/hep-ph/9806404)]:

$$f(x, Q_0^2 = 0.26 \text{ GeV}^2) = Nx^a(1-x)^b(1 + A\sqrt{x} + Bx)$$

and evolve to higher scales using the QCDNUM program. The parameters are fixed by flavour- and momentum sum relations, and some heuristic guesses. In particular, heavier valence quarks should have larger x , as they must all have similar velocities in order for the hadron to stay intact.

Parton distribution functions



- ▶ $\langle x \rangle$ is higher for heavy valence content (solid lines), and correspondingly lower for light content (dashed lines).

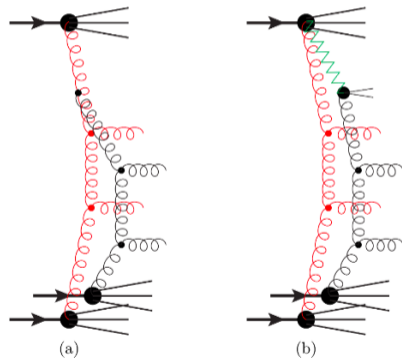
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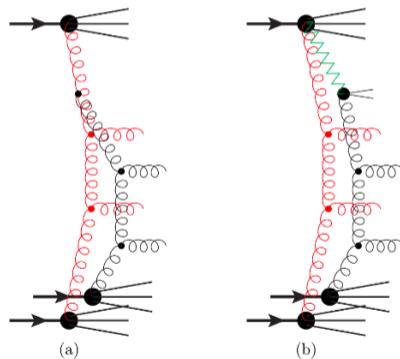
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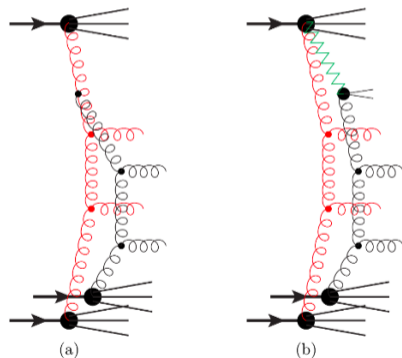
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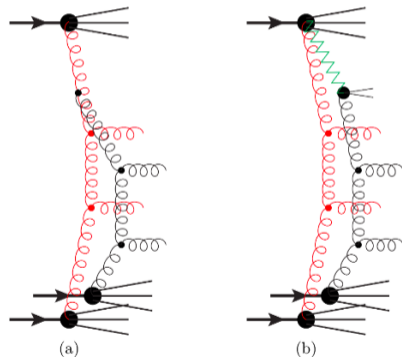
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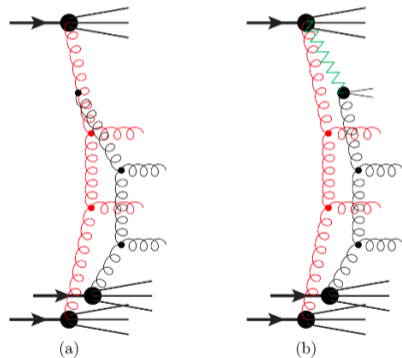
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- ▶ Secondary absorptive collisions are modelled like diffractive interactions.
- ▶ Combine partons from all subevents, then do color reconnection, string interactions, string hadronization, etc.



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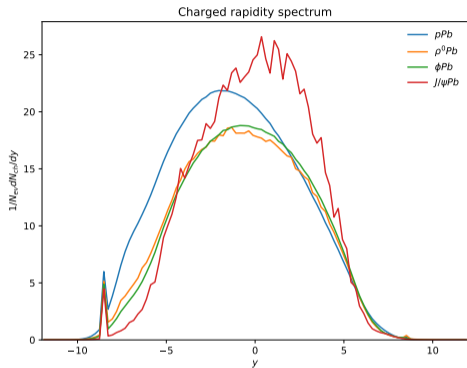
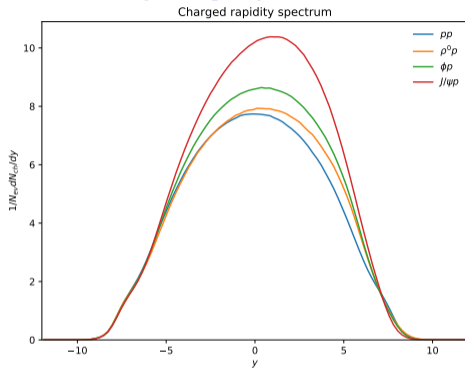
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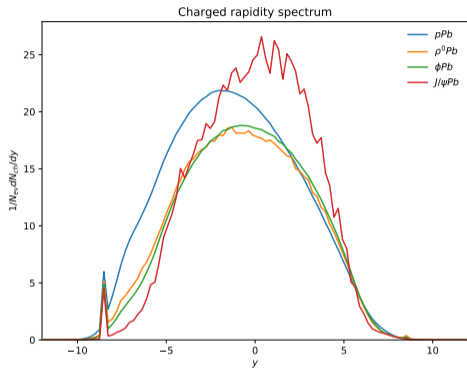
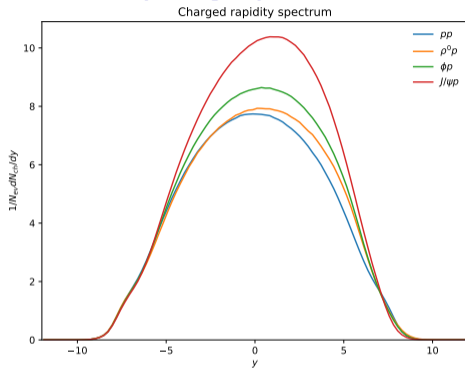
Applying this procedure to the asymmetric meson-nucleon case gives mediocre results. The fitting targets are insensitive to asymmetric fluctuations. Furthermore, the model gives unphysically large fluctuations for J/ψ , which is expected to have a small wavefunction. Clearly there is room for improvement.

Model test: Rapidity spectra at 5.02 TeV



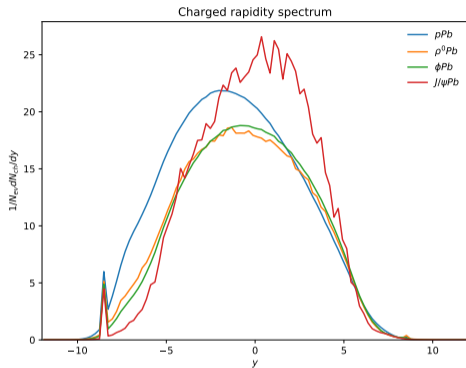
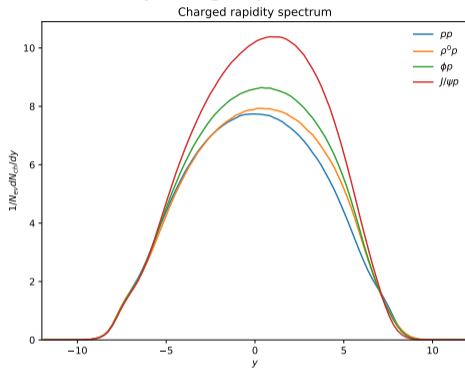
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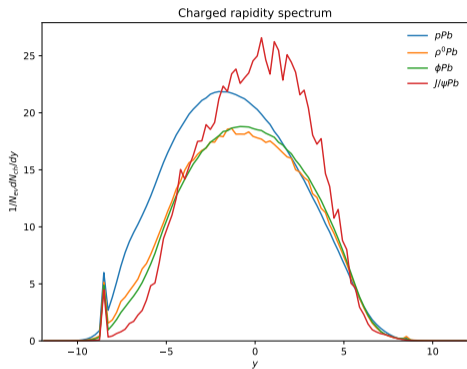
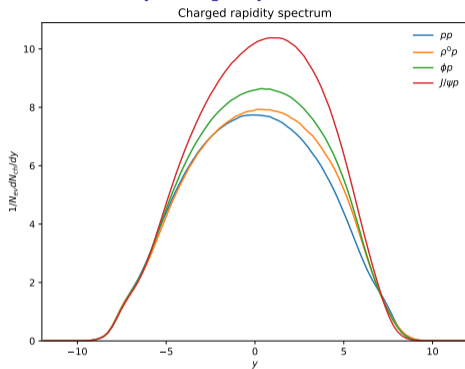
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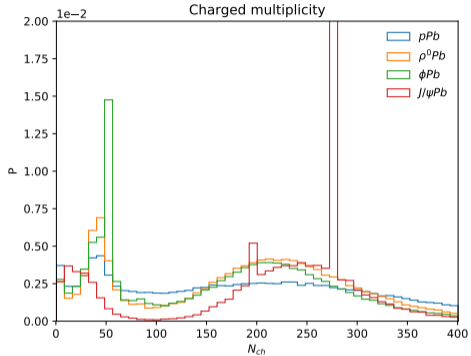
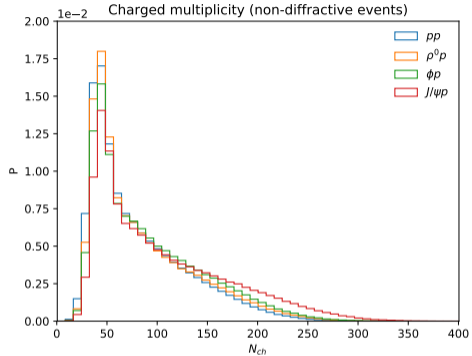
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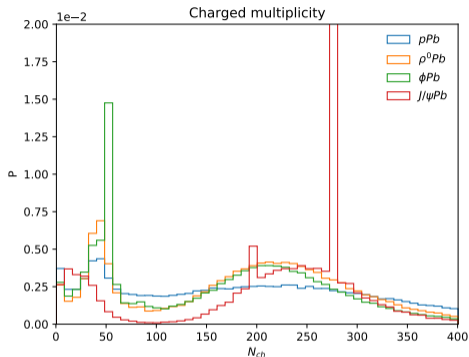
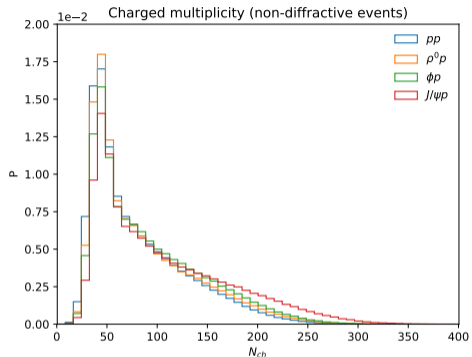
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- ▶ pPb has more subcollisions, and is thus pushed harder in the ion-going direction.
- ▶ Due to fluctuations and impact parameter sampling, J/ψ gets some events with extremely high weight.

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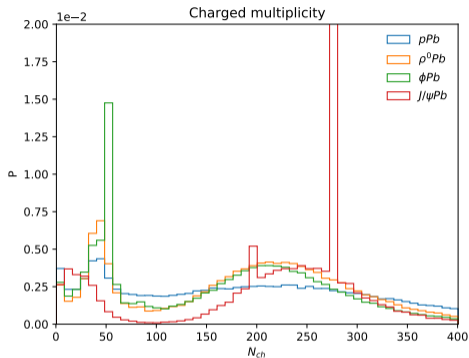
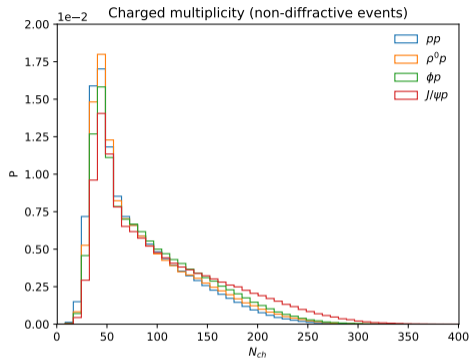
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- ▶ Long proton tail is driven by larger cross section and more subcollisions.
- ▶ Heavier mesons produce fewer subcollisions, but each subcollision produces more particles, leading to a non-trivial progression from ρ^0 to ϕ to J/ψ .

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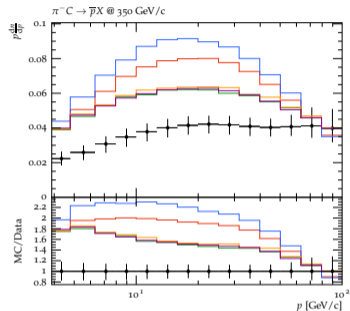
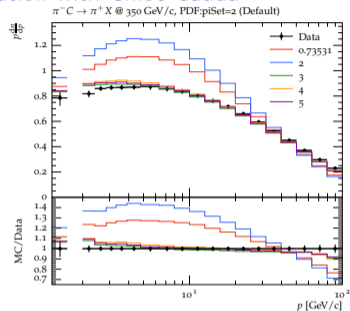
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$\pi^- C$ at NA61/SHINE [arXiv:2209.10561v1]

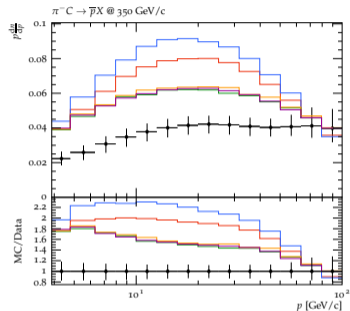
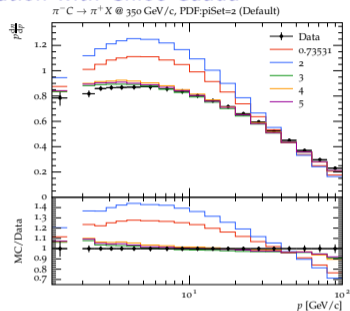
In collaboration with Chloé Gaudu



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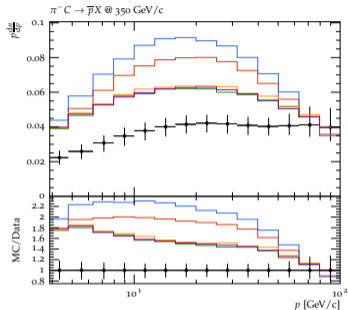
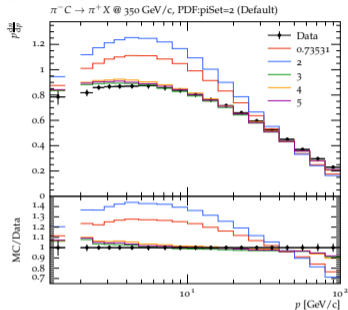
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- ▶ ANGANTYR shows good agreement in meson spectra.

$\pi^- C$ at NA61/SHINE [arXiv:2209.10561v1]

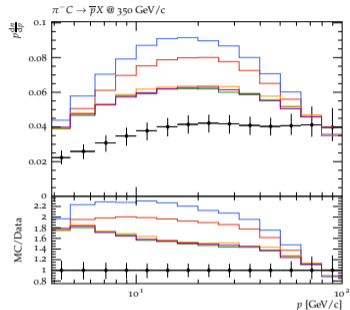
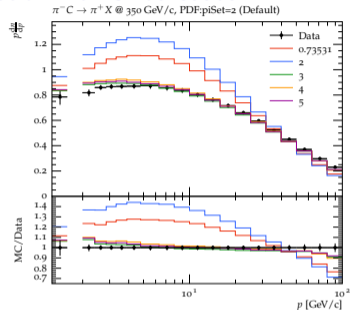
In collaboration with Chloé Gaudu



- ▶ The different colours refer to different values of the $p_{0,\perp}^{\text{ref}}$ parameter, which represents a saturation scale in MPI evolution.
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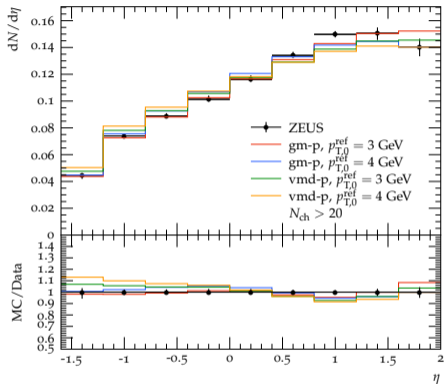
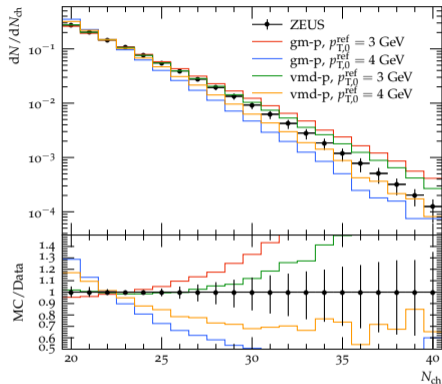
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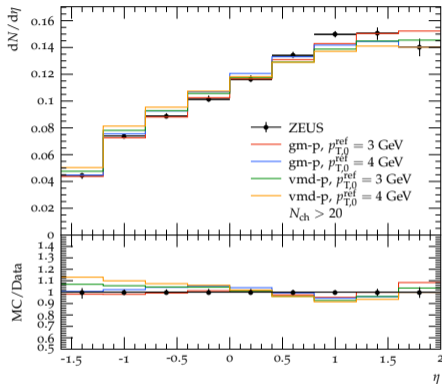
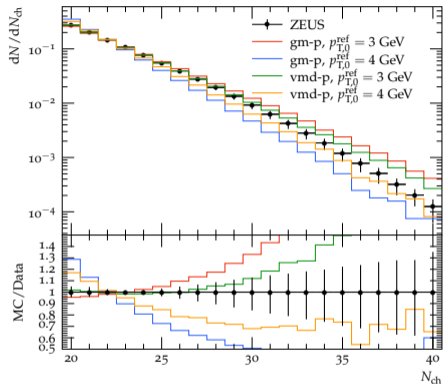
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- ▶ Low energy framework is not applied here.

γp at HERA [arXiv:2106.12377]



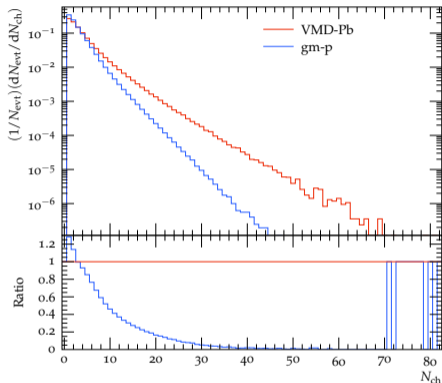
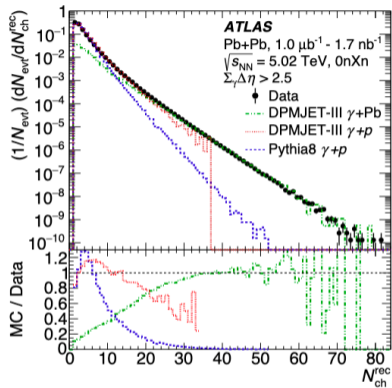
► The $p_{0,\perp}^{ref}$ variation gives a sense of the model uncertainty.

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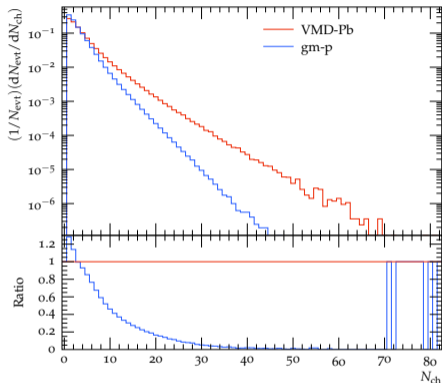
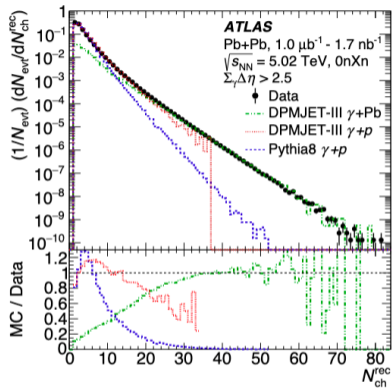
- ▶ The $p_{0,\perp}^{ref}$ variation gives a sense of the model uncertainty.
- ▶ The shift due to changing $p_{0,\perp}^{ref}$ is larger on average in the full photoproduction than in just the VMD component.

ATLAS $\gamma + \text{Pb}$ multiplicities [arXiv:2101.10771]



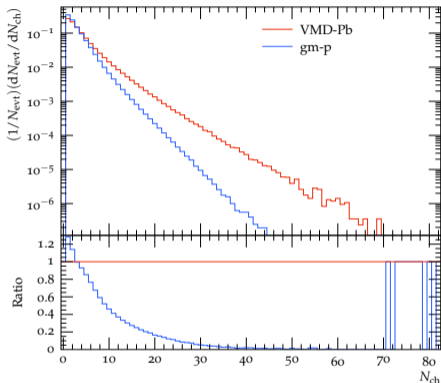
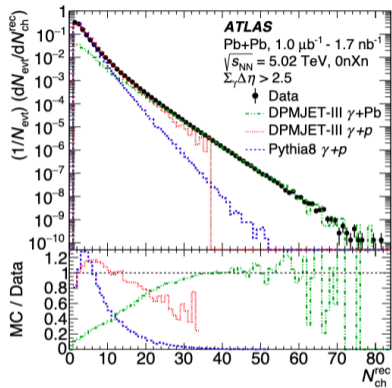
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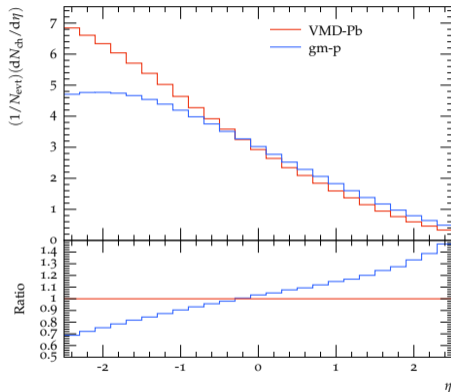
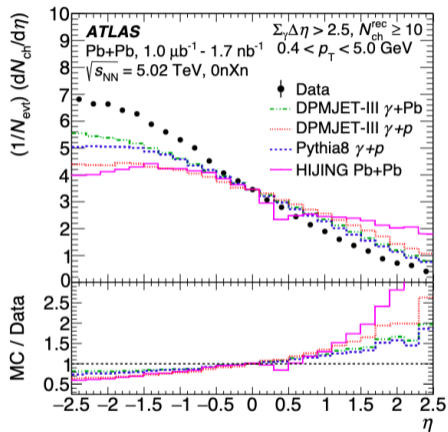
- ▶ The ATLAS data is not corrected for the limited efficiency, estimated to $\sim 80\%$.
- ▶ Qualitatively speaking, the shift from γp to γPb is consistent with data.

ATLAS $\gamma + Pb$ multiplicities [arXiv:2101.10771]



- ▶ The ATLAS data is not corrected for the limited efficiency, estimated to $\sim 80\%$.
- ▶ Qualitatively speaking, the shift from γp to γPb is consistent with data.
- ▶ In γp , the VMD component has less average multiplicity than in full photoproduction. This could be the other way around for γPb .

ATLAS eta spectrum [arXiv:2101.10771]



- ▶ Again, we cannot make a direct comparison, but the fit is still good when accounting for the limited efficiency in the multiplicity cut.

Outline

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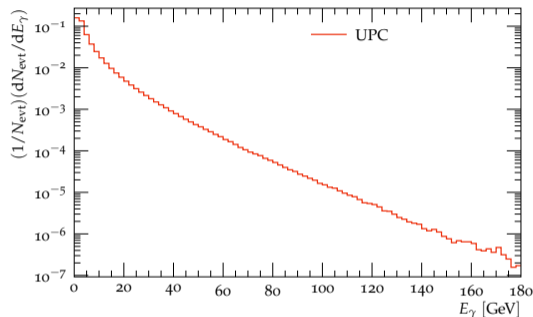
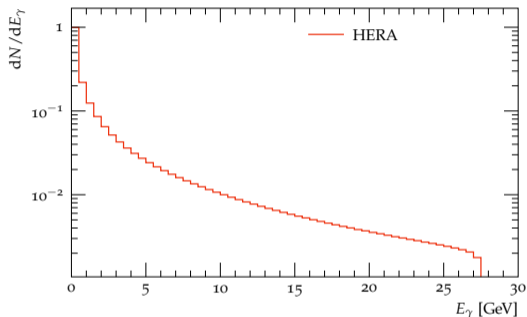
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- ▶ Room for other details, such as low-energy modelling.
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- ▶ Our model shows a good agreement with data from NA61/SHINE, HERA, and ATLAS UPCs.

Outline

Backup slides

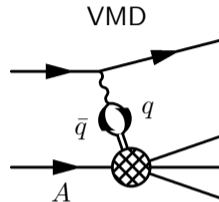
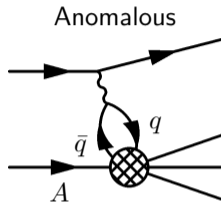
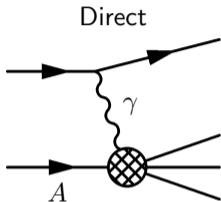
Photon flux [arXiv:1901.05261]



$$f_{\gamma/e}(x) = \frac{\alpha_{EM}}{2\pi} \frac{1 + (1-x)^2}{x} \log \left[\frac{Q_{\max}^2 (1-x)}{m_2^2 x^2} \right]$$

$$f_{\gamma/A}(x) = \frac{\alpha_{EM} Z^2}{\pi x} [2\xi K_1(\xi) K_0(\xi) - \xi^2 (K_1^2(\xi) - K_0^2(\xi))]$$

Photon wavefunction details [arXiv:hep-ph/9403393]



$$|\gamma\rangle = c_{\text{bare}} |\gamma_{\text{bare}}\rangle + \sum_q c_q |q\bar{q}\rangle + \sum_{V=\rho^0, \omega, \phi, J/\psi} c_V |V\rangle$$

$$c_V = \frac{4\pi\alpha_{EM}}{f_V^2}$$

V	$f_V^2/4\pi$
ρ^0	2.20
ω	23.6
ϕ	18.4
J/ψ	11.5

$p_{0,\perp}^{\text{ref}}$ variations

